

# Evaluating the effect of Non-Uniform Subsidence on Behave of Steel Cooling Towers under Wind Load

Shahryar Heidari\* and Abdulrahim Jalali

Department of Civil engineering, Maragheh Branch, Islamic Azad University, Maragheh, Iran;  
shahryar\_haidari@yahoo.com, Jalali@tabrizu.ac.ir

## Abstract

**Background/Objectives:** This study was aimed to evaluate the effect of non-uniform subsidence on behave of steel cooling towers under wind load. **Methods/Statistical Analysis:** This study was done through Kato model and tower behave was studied after applying different loads. The tower height is 170 meters above the ground. The maximum radius was 60 meters at the bottom and the minimum radius was 36.5 in the upper part. Then the tower behavior were analyzed under loading in nonlinear static load cases. **Findings:** The results showed that the steel cooling tower had elastic behavior against the wind but components of lower levels of tower had plastic behaviour and eventually will lead to the destruction of the tower. Also the most tensions occurs in the columns. Most effect and increasing of tension occurs in columns with increasing the wind load. Balances No 5, 8, 15 are best balances for implementation the stiffener.

**Keywords:** Cooling Towers, Non-Uniform, Steel, Wind Load

## 1. Introduction

Low subsidence in soil under the foundation of a structure or rotating foundation and structures (like a rigid material) won't create new tensions in the structure. But non-uniform subsidence of foundation can create considerable tension in structures and foundation. As a result, non-uniform subsidence is considered as a structural loading. So in different regulations of structures designing, there are coefficients for considering corresponding troops with non-uniform subsidence of structures and its combining with other loading factors. The difference of subsidence in the sandy soil is approximately equal to the maximum subsidence but in clay soil the difference of subsidence is lower than maximum subsidence<sup>1</sup>. Cooling towers are one of the great human inventions and due to the specific issues in the analysing and designing are interesting for researchers and engineers. In thermal power plants, power generation and petrochemicals, machines heat should be transferred to the external environment to prevent increasing the temperature in different parts of the plant. One of empirical research in field of non-uniform subsidence was done by<sup>2</sup>. Rao studied non-uniform subsidence too (1992)<sup>3</sup>. Akhtari studied non-uniform

subsidence through provided formula by Kato and Matza on mathematical model  $\omega = \Delta U \cos(n\theta)$  in arak cooling tower<sup>4</sup>. Kato et al., studied critical internal forces in various modes and noted that tensions were decreased highly in all parts compared with linear mode but the deformation of tower was increased<sup>5</sup>. This study was aimed to evaluate the effect of non-uniform subsidence on behave of steel cooling towers under wind load.

## 2. Materials and Methods

This research was done through Kato model and tower behave was studied after applying different loads. The geometry of tower is as follows:

The tower height is 170 meters above the ground. The maximum radius was 60 meters at the bottom and the minimum radius was 36.5 in the upper part. Tower had hyperbolic shape to height of 122 meters and it had cylinder shape to height of 170 meters after the balance. Equation of each balance radius of the tower is as follows:

$$r = \begin{cases} 36.5 \sqrt{1 + \left(\frac{z-122}{c}\right)^2} & x < 0 \\ 36.5 & x \geq 0 \end{cases} \quad (1)$$

\* Author for correspondence

Z: tower balance of the ground, C: radius of curvature of the hyperbolic tower = 93.51. Tower geometry is shown in Figure 1<sup>5</sup>.

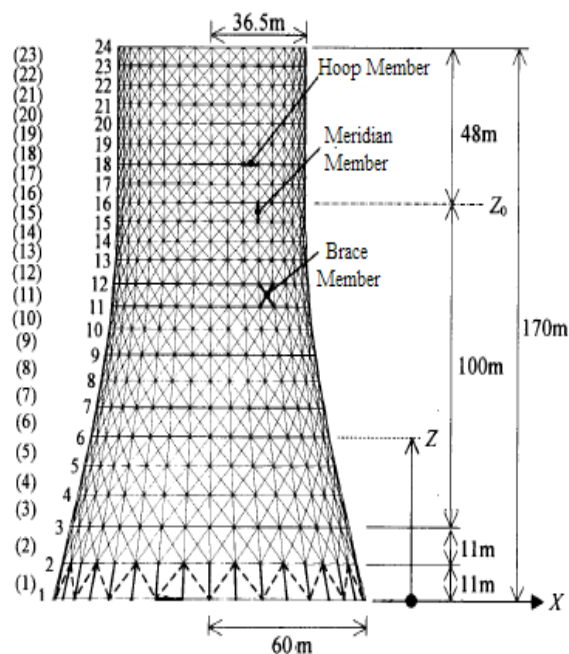


Figure 1. Geometry of cooling tower<sup>5</sup>.

Table 1. Specification of cooling towers sections<sup>5</sup>

| Member              | Balance | Cross section (Cm <sup>2</sup> ) | Moment of inertia (Cm <sup>4</sup> ) |
|---------------------|---------|----------------------------------|--------------------------------------|
| (Hoop Members)      | H24-24  | 96.3                             | 59000                                |
|                     | H16-23  | 74.4                             | 23100                                |
|                     | H06-15  | 40.2                             | 8050                                 |
|                     | H04-05  | 80.4                             | 16100                                |
|                     | H02-03  | 364                              | 256850                               |
| (Meridional Member) | M17-23  | 33.7                             | 4100                                 |
|                     | M11-16  | 109                              | 40600                                |
|                     | M08-10  | 149.2                            | 66000                                |
|                     | M02-07  | 200.2                            | 159000                               |
|                     | M01     | 280                              | 336500                               |
| (Brace Member)      | B20-23  | 33.7                             | 4100                                 |
|                     | B16-19  | 50                               | 6070                                 |
|                     | B03-15  | 80.4                             | 16100                                |
|                     | B02     | 88.6                             | 21900                                |
|                     | B01     | 87.5                             | 26900                                |

Due to the length of used parts in steel cooling towers, the members should possess high ziration radius to keep emaciation in limit. Truss compound tools were used

to acheieve this purpose, but these tools were inchmeal replaced by the weight of used steel were decreased due to using of tubular sections in cooling tower. All of segment are tubular sections in *Kato* model. Profile of used sections are mentoined in Table 1<sup>5</sup>. Beams and columns are rigidly connected to each other in *Kato* model. The connecting of bracing members is in articulation type and the members are connected in the middle part so that buckling length is reduced by half. Columns and braces are connected to each other in articulation type infirst row and the members also act axially.

Type of used steel in the profiles of the cooling tower is “steel ST-37” with yield stress 2,400 kN/cm<sup>2</sup> and modulus of elasticity is 2,000,000 kgN/cm<sup>2</sup>.

## 2.1 Buckling of Compression Members

One of the most important issues in structures is buckling in the pressure member. Euler equation was used for controlling of buckling of cooling tower members so this equation is presented as maximum thrust force of pressure ( $P_{cr}$ ) for each member.

$$P_{cr} = \frac{\pi^2 EI}{L_e^2} \quad (2)$$

Assuming a uniform axial stress in each member:

$$\sigma_{cr} = \frac{\pi^2 EI}{AL_e^2} \quad (3)$$

$L_e$  is the effective length depending on the support conditions. Support and values of effective length for different support conditions is presented<sup>6</sup>.

According to Figure 2,  $L_e$  is effective length for bracing members in fact the support conditions of beams and columns were between (1) and (2) status, also due to this issue, effective length for each member is 0.075  $L$ . According to equation (3) and Table 1, calculated values of  $\sigma_{cr}$  for all members is provided in Tables 2 to 4.

According to obtained values of  $\sigma_{cr}$  compressive stress didn't reach to step buckling before submission in all members  $\left( 2400 \frac{kgf}{cm^2} = yield \sigma > critical \sigma \right)$ .

In other words, all members of the towers are thick and there wasn't any problem in terms of elastic buckling instability during the loading.

**Table 2.** Buckling stress values in beams of cooling tower

| Balance | Columns    |                                  |                                      |                                       |
|---------|------------|----------------------------------|--------------------------------------|---------------------------------------|
|         | Length (m) | Cross section (Cm <sup>2</sup> ) | Moment of inertia (Cm <sup>4</sup> ) | Buckling stress (KNcm <sup>-2</sup> ) |
| 1       | 11.12      | 363                              | 256850                               | 20012                                 |
| 2       | 10.49      | 363                              | 256850                               | 22490                                 |
| 3       | 9.95       | 80.4                             | 16100                                | 7102                                  |
| 4       | 9.48       | 80.4                             | 16100                                | 7816                                  |
| 5       | 9.05       | 40.2                             | 8050                                 | 8589                                  |
| 6       | 8.68       | 40.2                             | 8050                                 | 9317                                  |
| 7       | 8.35       | 40.2                             | 8050                                 | 10070                                 |
| 8       | 8.06       | 40.2                             | 8050                                 | 10828                                 |
| 9       | 7.79       | 40.2                             | 8050                                 | 11565                                 |
| 10      | 7.57       | 40.2                             | 8050                                 | 12247                                 |
| 11      | 7.42       | 40.2                             | 8050                                 | 12769                                 |
| 12      | 7.30       | 40.2                             | 8050                                 | 13193                                 |
| 13      | 7.23       | 40.2                             | 8050                                 | 13460                                 |
| 14      | 7.18       | 40.2                             | 8050                                 | 13625                                 |
| 15      | 7.17       | 74.4                             | 23100                                | 21213                                 |
| 16      | 7.17       | 74.4                             | 23100                                | 21213                                 |
| 17      | 7.17       | 74.4                             | 23100                                | 21213                                 |
| 18      | 7.17       | 74.4                             | 23100                                | 21213                                 |
| 19      | 7.17       | 74.4                             | 23100                                | 21213                                 |
| 20      | 7.17       | 74.4                             | 23100                                | 21213                                 |
| 21      | 7.17       | 74.4                             | 23100                                | 21213                                 |
| 22      | 7.17       | 74.4                             | 23100                                | 21213                                 |
| 23      | 7.17       | 96.3                             | 59000                                | 41859                                 |

**Table 3.** Buckling stress values in columns of cooling tower

| Balance | Columns    |                                  |                                      |                                       |
|---------|------------|----------------------------------|--------------------------------------|---------------------------------------|
|         | Length (m) | Cross section (Cm <sup>2</sup> ) | Moment of inertia (Cm <sup>4</sup> ) | Buckling stress (KNcm <sup>-2</sup> ) |
| 1       | 11.50      | 280                              | 336500                               | 31899                                 |
| 2       | 11.46      | 200.2                            | 159000                               | 21224                                 |
| 3       | 10.38      | 200.2                            | 159000                               | 25870                                 |
| 4       | 9.31       | 200.2                            | 159000                               | 32177                                 |
| 5       | 9.27       | 200.2                            | 159000                               | 32428                                 |
| 6       | 8.21       | 200.2                            | 159000                               | 41369                                 |
| 7       | 8.18       | 200.2                            | 159000                               | 41696                                 |
| 8       | 8.14       | 149.2                            | 66000                                | 23413                                 |
| 9       | 8.11       | 149.2                            | 66000                                | 23604                                 |

|    |      |       |       |       |
|----|------|-------|-------|-------|
| 10 | 8.08 | 149.2 | 66000 | 23788 |
| 11 | 7.05 | 109   | 40600 | 26335 |
| 12 | 7.03 | 109   | 40600 | 26473 |
| 13 | 6.01 | 109   | 40600 | 36170 |
| 14 | 6.00 | 109   | 40600 | 36258 |
| 15 | 6.00 | 109   | 40600 | 36302 |
| 16 | 6.00 | 109   | 40600 | 36308 |
| 17 | 6.00 | 33.7  | 4100  | 11859 |
| 18 | 6.00 | 33.7  | 4100  | 11859 |
| 19 | 6.00 | 33.7  | 4100  | 11859 |
| 20 | 6.00 | 33.7  | 4100  | 11859 |
| 21 | 6.00 | 33.7  | 4100  | 11859 |
| 22 | 6.00 | 33.7  | 4100  | 11859 |
| 23 | 6.00 | 33.7  | 4100  | 11859 |

**Table 4.** Buckling stress values in braces of cooling tower

| Balance | Braces     |                                  |                                      |                                       |
|---------|------------|----------------------------------|--------------------------------------|---------------------------------------|
|         | Length (m) | Cross section (Cm <sup>2</sup> ) | Moment of inertia (Cm <sup>4</sup> ) | Buckling stress (KNcm <sup>-2</sup> ) |
| 1       | 8.11       | 87.5                             | 26900                                | 9226                                  |
| 2       | 8.00       | 88.6                             | 21900                                | 7625                                  |
| 3       | 7.77       | 80.4                             | 16100                                | 6549                                  |
| 4       | 7.19       | 80.4                             | 16100                                | 7650                                  |
| 5       | 6.64       | 80.4                             | 16100                                | 8957                                  |
| 6       | 6.48       | 80.4                             | 16100                                | 9425                                  |
| 7       | 5.97       | 80.4                             | 16100                                | 11073                                 |
| 8       | 5.84       | 80.4                             | 16100                                | 11573                                 |
| 9       | 5.73       | 80.4                             | 16100                                | 12051                                 |
| 10      | 5.62       | 80.4                             | 16100                                | 12496                                 |
| 11      | 5.54       | 80.4                             | 16100                                | 12893                                 |
| 12      | 5.12       | 80.4                             | 16100                                | 15106                                 |
| 13      | 5.07       | 80.4                             | 16100                                | 15404                                 |
| 14      | 4.70       | 80.4                             | 16100                                | 17897                                 |
| 15      | 4.68       | 80.4                             | 16100                                | 18044                                 |
| 16      | 4.67       | 50                               | 6070                                 | 10971                                 |
| 17      | 4.67       | 50                               | 6070                                 | 10972                                 |
| 18      | 4.67       | 50                               | 6070                                 | 10972                                 |
| 19      | 4.67       | 50                               | 6070                                 | 10972                                 |
| 20      | 4.67       | 33.7                             | 4100                                 | 10996                                 |
| 21      | 4.67       | 33.7                             | 4100                                 | 10996                                 |
| 22      | 4.67       | 33.7                             | 4100                                 | 10996                                 |
| 23      | 4.67       | 33.7                             | 4100                                 | 10996                                 |

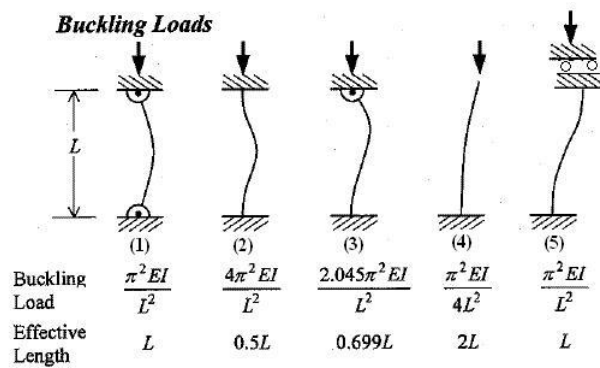


Figure 2. Figure of buckling load and the effective length for different support types<sup>6</sup>.

## 2.2 Modeling in Abaqus Software

Abaqus software was used for modeling the steel cooling tower between CSI, Abaqus, and OpenSEES<sup>7</sup>. In this research, steel was defined by using “steel101” recipes. The stress-strain diagram of steel is presented in Figure 3. All of defined sections are fiber section type in model. Modeled sections by Fiber are the most complete sections which determine properties of finite element sections by using the fibers well. Figure 4 indicated a sample of fiber element sections which defined in tower<sup>8</sup>. Existence changing location of different member is reason of one factor of non-linear behave structures which caused extra forces P-Δ force in member. Another factor of the behave is changing location of nodes compared to the initial status. Usually the software considers the effects of changing the location as stiffness matrix addition the main stiffness matrix which called the geometric stiffness matrix. Option P-Δ should be selected in Abaqus software to consider the effects of P-Δ in section of definition the geometric stiffness matrix. Option *corotational* should be selected for considering the simultaneous effects P-Δ and shift nodes. *Corotational* geometric stiffness matrix was used in studied model.

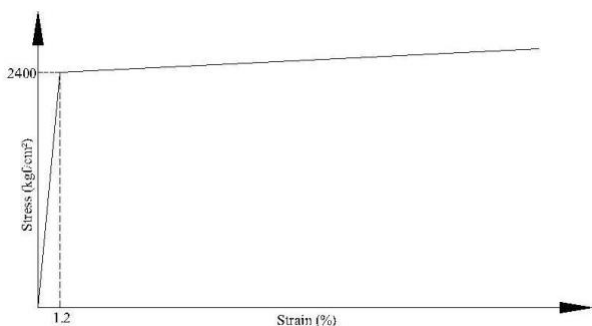


Figure 3. Diagram stress-strain of used steel in cooling tower.

Nonlinear beam column was used for defining the elements of cooling tower. This element is one of the most complete non-linear elements in Abaqus software. It determined the plastic hinge along the length of member by defining a series of plastic joint.

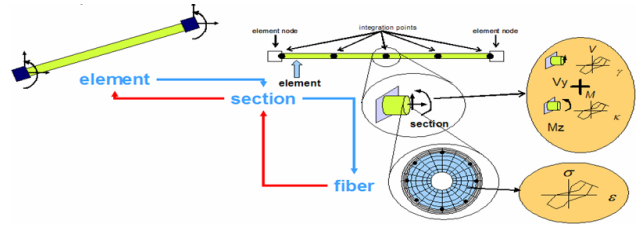


Figure 4. Model fiber section in cooling tower<sup>8</sup>.

## 3. Results and Discussion

The wind load created the most tensions in members and it is determinative load in metal cooling tower. VGB regulations is one of the most respected regulations for designing the cooling tower. The instruction of the regulations in wind loading is as follows<sup>9</sup>:

Wind load applied to each point of the cooling tower can be obtained from the following equation:

$$W(z, \theta) = \phi \cdot q_0(z) \cdot c_p(\theta) \quad (4)$$

In the above equation:  $\phi$  is dynamic magnification factor to consider the dynamic effects of wind load which it is calculated according to diameter of gorge, minimum natural frequency of tower and wind pressure on the edge of the tower. There isn't any formula for metal cooling tower. The dynamic magnification factor is 1 value in this research.

(z)  $Q_0$  is base wind pressure in balance z of cooling tower. The instruction of VGB regulations is used for calculating  $q_0(z)$  on base of regulations 5 in the regulations, z is the height of each part of tower compared to the base level.

$$Q_0(z) = 0.9 \times \left( \frac{z}{100} \right)^{0.22} \frac{kN}{m^2} \quad (5)$$

$C_p(\theta)$  is coefficient of pressure distribution on the circumference of the shell. The coefficient is calculated in VGB instruction in terms of cover surface roughness (Table 5). According to the metal cooling tower is covered by corrugated sheets No 1, k/a or surface roughness is a great number on base of Figure 5 so K1.0 curve is used for

calculating  $C_p(\theta)$  (Table 6). Therefore, in this research the relation 6 is used to calculate  $C_p(\theta)$

$$C_p(\theta) = \begin{cases} 1 - 2.0 \left( \sin \frac{90}{70} \theta \right)^{2.267} & ; 0 \leq \theta \leq 70 \\ -1 + 0.5 \left\{ \sin \left[ \frac{90}{21} (\theta - 70) \right] \right\}^{2.395} & ; 70 \leq \theta \leq 90 \\ -0.5 & ; 90 \leq \theta \leq 180 \end{cases} \quad (6)$$

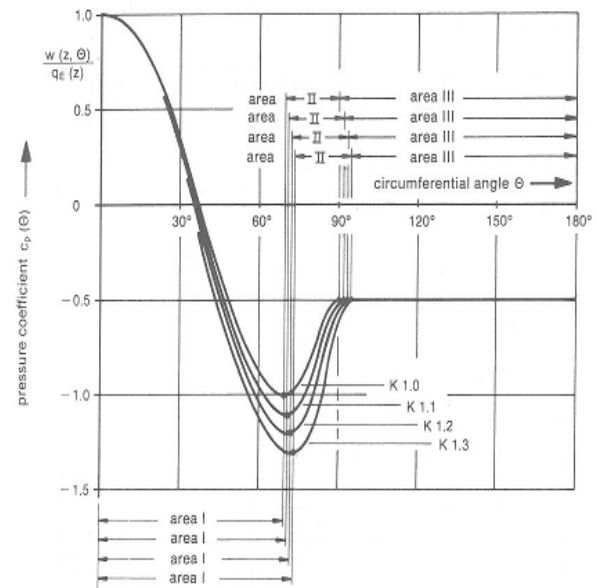
**Table 5.** Table of curves pressure distribution as a function of surface roughness<sup>9</sup>

| Roughness      | Minimum pressure<br>(min $C_p$ ) | Curve |
|----------------|----------------------------------|-------|
| 0.006 to 0.010 | -1.3                             | K 1.3 |
| 0.010 to 0.016 | -1.2                             | K 1.2 |
| 0.016 to 0.025 | -1.1                             | K 1.1 |
| 0.025 to 0.100 | -1.0                             | K 1.0 |

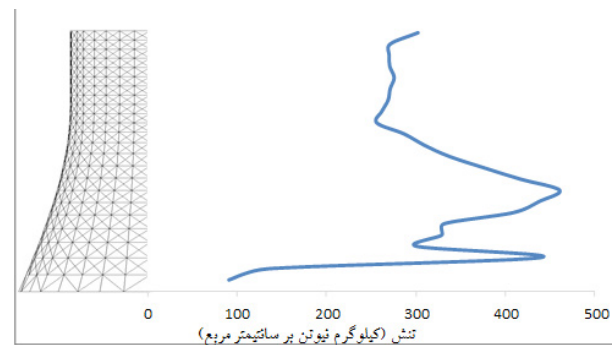
Usually, the most transformations occurs against the wind load in cooling tower. The calculated wind load by using VBG regulations in each balance and each angle was centralized on base of the load level of each node in the radial direction. The caused tension by wind load of structural members are provided at different heights in this section. The results are presented in Figures 6 to 12 in absolute value status.

According to diagrams 6 to 8 under the effect of wind load, the tensions of all members is in elastic range. the created tensions in the columns on the most critical balance: 60%  $\sigma_y$ , in braces about:30% and in beams about:20%  $\sigma_y$ . There are some fractures in altitudinal distribution of tensions as the charts show. The fractures were created due to sudden changes in cross-section of members similar behavior against gravity load and against wind load. For example the most prominent point of fracture Figure 6 occurred in level 4 of altitudinal distribution of beams. In this level the cross section was decreased to about 80% from floor 3 to 4 and lead to sudden increasing of tension. In this study for better understanding the behave of the tower againsts the increasing wind load, the load was incrementally applied to tower for magnification factor of different wind load ( $q$ ) and the results of tensions were calculated and presented in Figures 9 to 12.

To increase reliability of structure againsts the loads, stiffener can be used at critical levels. These balances posses higher transience so balances No 5, 8, and 15 are best balances for implementation the stiffener. Even though, the gust factor decreases with the increase in height of water tower, the gust pressures increase with height of the water tower. The same is also valid for multistoried tall frames<sup>10,11</sup>.



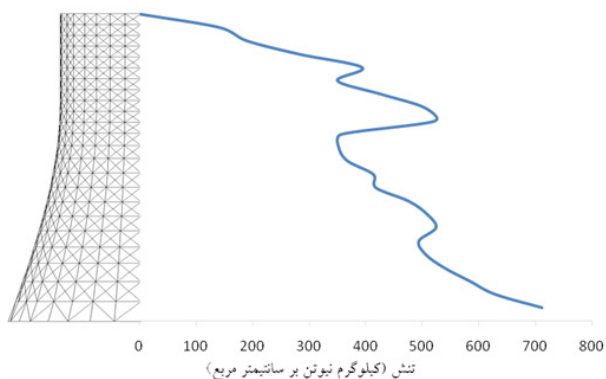
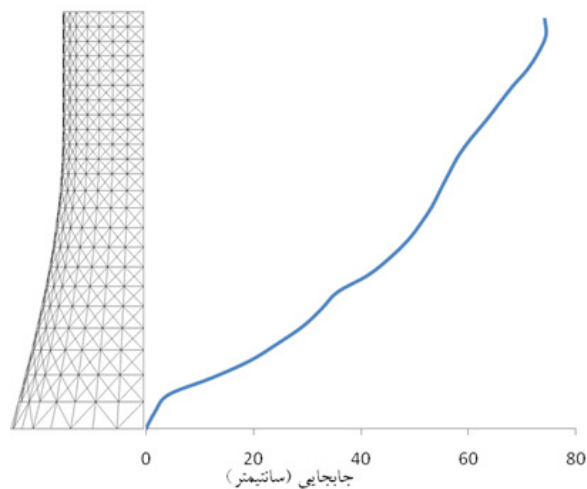
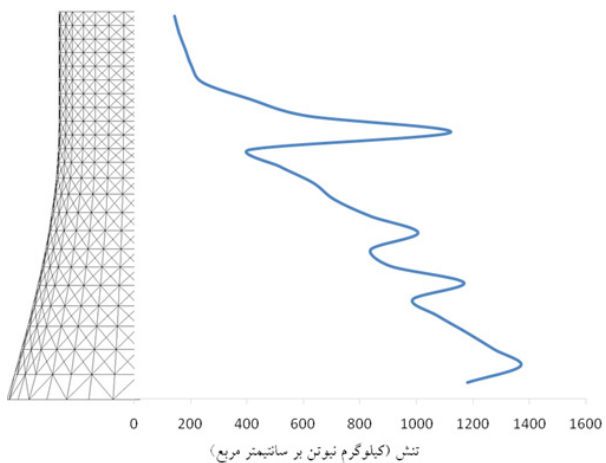
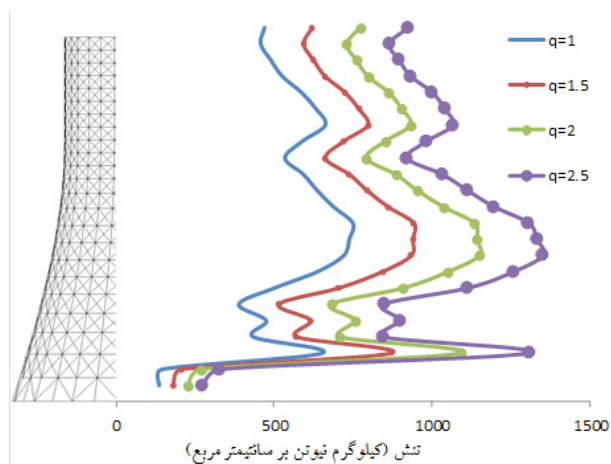
**Figure 5.** Amount of  $C_p(\theta)$  according to the VBG regulations<sup>9</sup>.

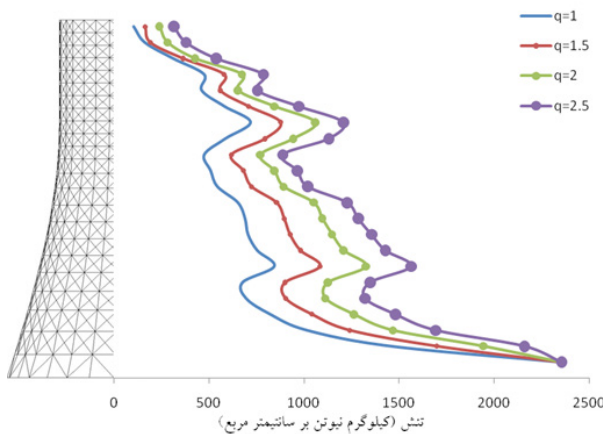


**Figure 6.** Axial tension of beams under the effect of wind load.

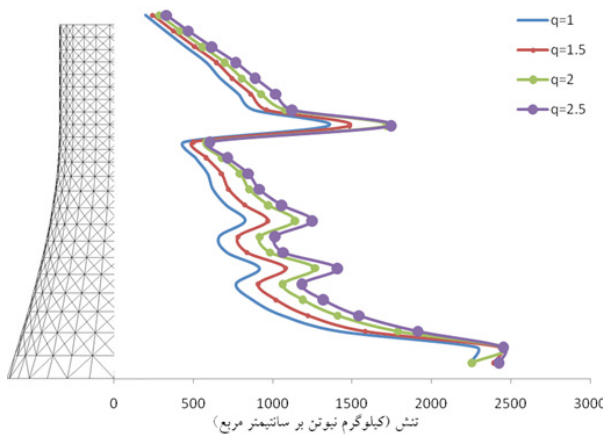
**Table 6.** Function of pressure curve CP ( $\theta$ )<sup>9</sup>

| Curve | Minimum pressure (min $C_p$ ) | Zone 1                                                    | Zone 2                                                        | Zone 3 | pressure |
|-------|-------------------------------|-----------------------------------------------------------|---------------------------------------------------------------|--------|----------|
| 1.3k  | 1.3                           | $-1.0+2.0\left(\sin\frac{90}{70}(\theta)\right)]^{2.267}$ | $-1.0+0.5\left[(\sin\frac{90}{21}(\theta-70))\right]^{2.395}$ | 0.5    | 0.66     |
| 1.2k  | -1.2                          | $-1.0+2.1\left(\sin\frac{90}{71}(\theta)\right)]^{2.239}$ | $-1.1+0.6\left[(\sin\frac{90}{22}(\theta-71))\right]^{2.395}$ | -0.5   | 0.64     |
| 1.1k  | -1.1                          | $-1.0+2.2\left(\sin\frac{90}{72}(\theta)\right)]^{2.208}$ | $-1.2+0.7\left[(\sin\frac{90}{23}(\theta-72))\right]^{2.395}$ | 0.5    | 0.60     |
| 1.0k  | -1.0                          | $-1.0+2.3\left(\sin\frac{90}{73}(\theta)\right)]^{2.068}$ | $-1.3+0.8\left[(\sin\frac{90}{24}(\theta-73))\right]^{2.395}$ | -0.5   | 0.56     |

**Figure 7.** Axial tension of braces under the effect of wind load.**Figure 9.** Lateral displacement of cooling tower under the effect of combined loads.**Figure 8.** Axial tension of columns under the effect of wind load.**Figure 10.** Axial stress of beams under the effect of combined loads for magnification factor of different load.



**Figure 11.** Axial stress of braces under the effect of combined loads for magnification factor of different load.



**Figure 12.** Axial stress of columns under the effect of combined loads for Magnification factor of different load.

## 4. Conclusion

Under the effect of wind load, the tension is in elastic range for total members. Also the most tensions occurs in the columns. Most effect and increasing of tension occur in columns with increasing the wind load. Balances No 5, 8, and 15 are best balances for implementation the stiffener. Sudden changes in cross-section of members causes the fractures of structures against the wind load.

## 5. Acknowledgment

This article is derived from a Master's thesis of Shahryar Haidari titled "Evaluating the effect of non-uniform subsidence on behavior of steel cooling towers under wind load. The authors appreciate the support received from the Islamic Azad University, Maragheh Branch of Tehran, Iran.

## 6. References

1. Tsytovich N. Soil Mechanics. Mir Publishers: Moscow, 1976.
2. Chesileski R, Cuminski A, Zak M. Large Settlement of Hyperboloidal Cooling Towers. Proceedings Conference on Large Ground Movement and Structures. UWIST. Cardiff. 1977. p. 672–86.
3. Rao SVKM, Rao TVSRA. Stress resultants in hyperboloid cooling tower shells subjected to foundation settlement. Computers and Structures. 1994 Aug 17; 52(4):813–27.
4. Akhtari A. Effects of asymmetric subsidence on power plant cooling towers mentioned, Khajeh Nasir Toosi University of Technology, Tehran. 2002; 145pp.
5. Kato S, Nakazawa S, Shimaoka S, Ohya T. Effectiveness of buckling restrained members for diagonal columns to reduce the seismic response of cooling towers. In Natural Draught Cooling Towers: Proceedings of the Fifth International Symposium on Natural Draught Cooling Towers, Istanbul, Turkey. 2004; 299pp.
6. Popov EP. Engineering mechanics of solids. Prentice Hall: Englewood cliffs New jersey, 1990.
7. Soroshnia S. The Complete Reference Software ABAQUS (advanced level, especially civil)., Negar Danesh. 2013; 234pp.
8. Gould PL. Differential settlement of hyperbolic cooling towers. Journal of the Structural Division. 1972 Oct; 98(10):2207–21.
9. Jacobs J, Schmidt KH. VGB Technische Vereinigung der Großkraftwerksbetreiber. VGB Technische Vereinigung der Grosskraftwerksbetreiber, 1986.
10. Kumar DB, Swami BLP. Wind effects on tall building frames-influence of dynamic parameters. Indian Journal of Science and Technology. 2010 May; 3(5):583–87.
11. Dean KB, Swami BLP. Wind effects on water towers-influence of various dynamic parameters. Indian Journal of Science and Technology. 2010 Aug; 3(8):911–15.