

# Analysis of Classical Controller by Variation of Inner-loop and Controller Gain for Two-level Grid-connected Converter

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## Abstract

With the depletion of fossil fuel, the world is shifting towards the sources of alternate energy, but a major impediment in their utilization is their inter-connection with the grid. This paper builds on the model of a grid-connected converter which is used to interface the different alternate energy sources using matlab/simulink as simulation software. The classical control techniques proportional/proportional integral (P/PI) are applied on the model of the two-level grid-connected converter with LCL filter. The overall structure of the system is based upon the inner-loop capacitor current and outer-loop controller feedback. These parameters are varied and their effect is investigated in the presence of utility harmonics. The limitations and performance of the system with the variation in gain values is studied so that optimal gains can be identified.

**Keywords:** Grid-Connected Converters, Micro-grid, Total Harmonic Distortion

## 1. Introduction

A micro-grid is a collection of the Distributed Energy Resources (DER) within the main grid, which can be used in both stand-alone and grid-connected mode<sup>1</sup> When the DER are connected to the grid utility using a two-level converter with a LCL filter, harmonics enter the system at the Point of Common Coupling (PCC) from the grid side due to low impedance provided by the LCL filter<sup>2</sup> The harmonics are significant at the odd multiples of the fundamental frequency (50Hz) and affect the system at the resonance frequencies. Reducing the Total Harmonic Distortion (THD) of the output current is the main objective of the controller. A lot of work has been carried out in this area<sup>3-13</sup> but still requires detailed analysis and alternative suitable controller.

There are two types of control systems (i) open-loop and (ii) closed-loop. A simple stepper motor which produces a certain torque in response to a certain voltage applied at its stator is an open-loop system. The Automatic Braking System (ABS) of a car is a closed-loop system which has a certain output feedback with which it compares the defined reference and attempts to minimize the error using a certain control action.

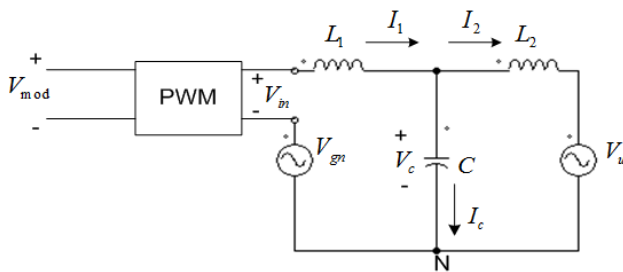
The limitation of conventional controllers like proportional P and proportional integral PI controllers is that they do not give good gain at the harmonic frequencies along with accurate reference tracking for a fast switching signal<sup>4</sup>. Our signal of interest is the grid current, which has a value of 100A (peak) and oscillates at a frequency of 50 Hz. We need a controller that has a very fast response and can suppress the harmonics at the odd

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frequencies, while simultaneously tracking the specified reference parameters<sup>5</sup>. In this regard, the performance of repetitive and the PR (Proportional Resonant) controllers have found to be more robust for real-time applications<sup>6</sup>.

## 2. Mathematical Modeling

We start the mathematical modeling of the three-phase two-level converter with a LCL filter at each phase. The system is complex so we start with a single-phase equivalent circuit of the two-level converter and derive its transfer function. We apply KVL to the two independent loops and KCL to the central node in Figure 1.



**Figure 1.** Single-phase equivalent of a three-phase two-level converter with LCL filter.

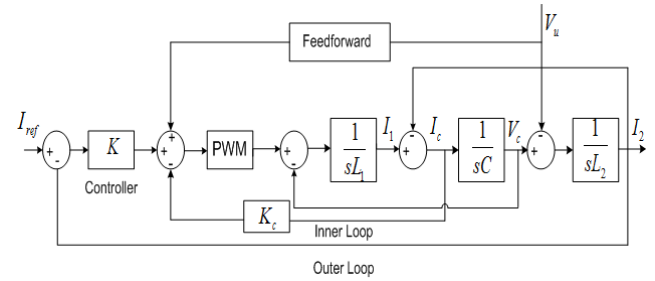
Here we have assumed that the ground-to-neutral voltage  $V_{gn} = (V_{an} + V_{bn} + V_{cn})/3$  is equal to zero, because the capacitors are connected to the DC link. The three phase-to-neutral voltages are  $V_{an}$ ,  $V_{bn}$  and  $V_{cn}$  respectively. We manipulate the KVL and KCL equations and make use of the Laplace transform<sup>8</sup> to get the output current  $I_2$  as

$$I_2(s) = \frac{V_{in}(s)}{s^3 L_1 L_2 C + s(L_1 + L_2)} - \frac{(s^2 L_1 C + 1)V_u(s)}{s^3 L_1 L_2 C + s(L_1 + L_2)} \quad (1)$$

We ignore the second part of this equation which is the disturbance injected into the system at the PCC, to derive the transfer function between the reference signal  $V_{in}(s)$  and the output signal  $I_2(s)$ . Henceforth, the open-loop transfer function of this system is

$$G(s) = \frac{I_2(s)}{V_{in}(s)} = \frac{1}{s^3 L_1 L_2 C + s(L_1 + L_2)} \quad (2)$$

Including an inner-loop gain  $K_c$  from  $I_c$  back to the summer provides a damping term and makes the system more stable<sup>7</sup>.



**Figure 2.** Modified block diagram with two-loop feedback.

The output current  $I_2$  of the modified system Figure 2 is

$$I_2(s) = \frac{V_m(s)}{(L_1 L_2 C)s^3 + (K_c L_2 C)s^2 + (L_1 + L_2)} - \frac{(L_1 C s^2 + K_c C s + 1)V_u(s)}{(L_1 L_2 C)s^3 + (K_c L_2 C)s^2 + (L_1 + L_2)} \quad (3)$$

$G_1(s)$ , which is the closed-loop transfer function of the two-level converter with LCL filter including the capacitive feedback damping is as (4)

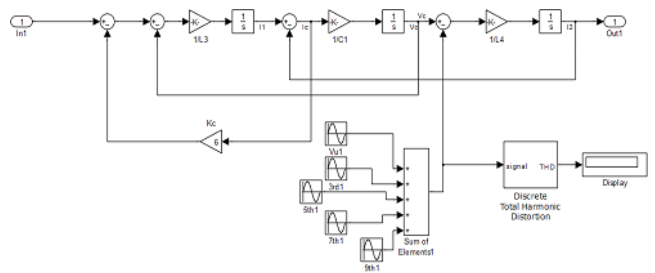
$$G_1(s) = \frac{1}{(L_1 L_2 C)s^3 + (K_c L_2 C)s^2 + (L_1 + L_2)s} \quad (4)$$

The utility disturbance is defined as (5)

$$D(s) = V_u (L_1 C s^2 + K_c C s + 1) \quad (5)$$

## 3. Matlab Simulations

The model used for simulation is shown in Figure 3, which is a linear approximation of the single-phase equivalent of the two-level grid-connected converter.



**Figure 3.** Simulink model of Two-Level Grid-Connected Converter.

The values of the components of the LCL filter are  $L_1=350\mu\text{H}$ ,  $L_2=50\mu\text{H}$  and  $C=22.5\mu\text{F}$ <sup>8</sup>. Substituting these values into (2), we find the poles of the transfer function which lie at 0 and  $\pm 3.1783i$  respectively. A system with a

pole at zero is a critically stable system. From Figure 4, it is clear that the system is critically stable and will become unstable when any input signal is given to it.

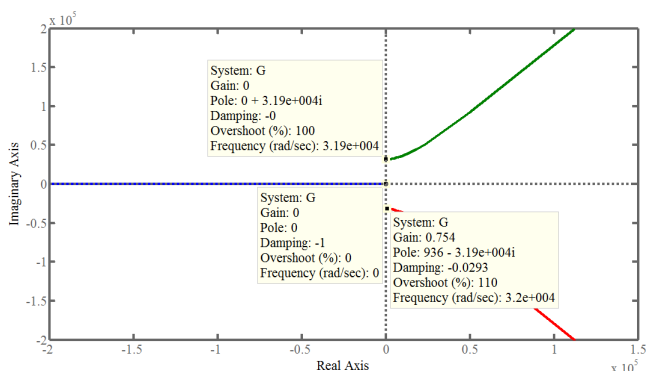


Figure 4. Root locus diagram of open-loop system G(s).

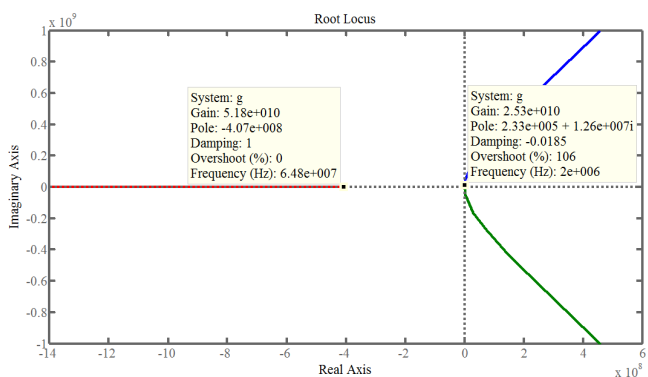


Figure 5. Root locus diagram of the closed-loop system G1(s).

From Figure 5, it is clear that the overshoot of our closed-loop system is less as compared to the open-loop systems and also that the bandwidth of the system has been increased due to the inclusion of the controller within the loop. Also, the damping has increased so the settling time of the system has decreased implying that the system has become more stable.

## 4. Proportional Controller

### 4.1 Effect of Inner-loop Gain $K_c$ on System Performance

The inner-loop gain  $K_c$  is varied and the resulting plots are recorded for a proportional controller (Figures 6,7), while the proportional gain  $K_p$  is kept constant at a value of 1.63. The reference tracking capabilities are increasing as the value of inner-loop gain  $K_c$  is increased from 0 - 1.4. From 1.6 - 3, we are getting the best possible results and

onward from 3, the THD in the output signal is increased although it still maintains good reference tracking. The THD injected into the system at PCC is 2.494%. For inner-loop gain  $K_c = 0$  our system is unstable. For inner-loop gain  $K_c = 1.4$  the system is stable but after 0.04 seconds, it starts getting unstable and THD in the signal is increasing. From Table 1, at inner-loop gain  $K_c$  equal to 1.6 we have reached our optimal performance as far as reference tracking is concerned.

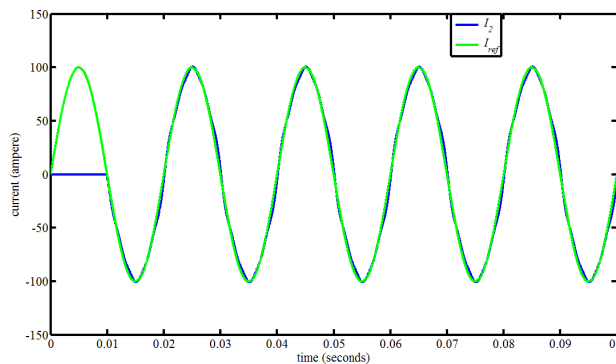


Figure 6. Plot of  $I(t)$  vs  $t$ , inner-loop gain  $K_c = 3$ .

At the value of inner-loop gain  $K_c$  equal to 3, we are getting the optimal phase margins and the gains margins along with a reduced value of THD. Figure 8, shows the bode plot of output current with respect to the reference current for the best controller gain at which the gain margins and phase margins are optimal. The results of our findings have been mentioned in Table 1.

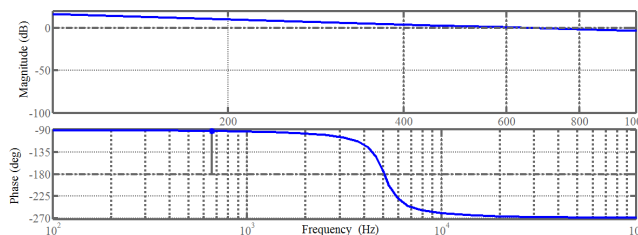


Figure 7. Bode plot of  $I_2$  w.r.t.  $I_{ref}$  for optimal gain i.e., inner-loop gain  $K_c = 3$ .

Table 1. Effect of variation of inner-loop gain  $k_c$  on system performance

S. No	$K_c$	THD	G.M (dB)	P.M ( $^\circ$ )	Stable
1	0	3804	undefined	-90	No
2	1.4	64.93	-0.161	-5.96	No
3	1.6	4.512	0.998	88.9	Yes
4	3	4.544	6.46	88	Yes
5	20	5.815	22.9	77	Yes

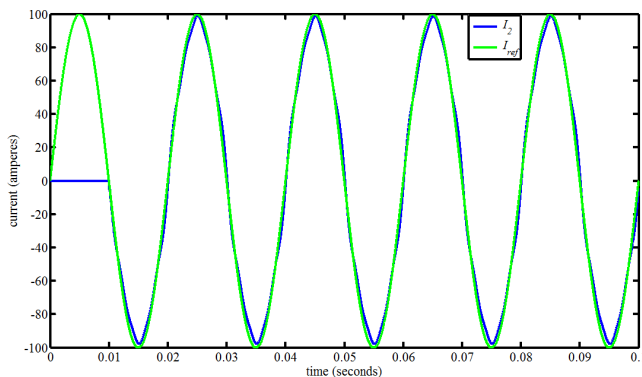
## 5. Proportional Integral Controller

This is basically the implementation of the Table 2 given in the paper<sup>8</sup>. We are varying the value of proportional gain  $K_p$  and integral gains  $K_I$  taking the inner-loop gain  $K_c = 3$ . With the increase in the value of the proportional gains  $K_p$  and integral gains  $K_I$  beyond the value of 1, the gain margins and phase margins are diminishing. The best performance of the controller is found at the value of 1.65. The bode diagram is shown in Figure 9.

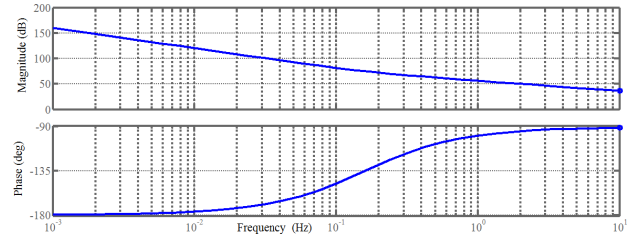
**Table 2.** Effect of variation of proportional  $K_p$  and integral  $K_I$  gains on thd

S.No	$K_p$	$K_I$	Gain Margin	Phase Margin (°)	THD	Stable
1	1	1	10.7	88.8	2.965	Yes
2	2	2	4.68	87.4	6.027	Yes
3	3	3	1.16	85.9	29.65	Yes
4	3.4	4	0.0726	1.92	45.81	Yes
5	3.5	4	-0.179	-3.9	18150	No
6	2.8	2.8	1.76	86.2	16.95	Yes
7	1.65	1.65	6.35	87.9	4.606	Yes

For proportional gain  $K_p =$  integral gain  $K_I = 1$ , the output is under-damped and  $I_2$  is over-exceeding the value of the reference current. The value of THD is less so the disturbance rejection is good. For proportional gain  $K_p =$  integral gain  $K_I = 2$ , the output signal is over-damped and the THD has increased. For proportional gain  $K_p =$  integral gain  $K_I = 3$ , the controller is able to follow the reference for the first cycle, but when a higher order disturbance enters the system at the beginning of the second cycle, the controller totally fails. For proportional gain  $K_p = 3.4$ , integral gain  $K_I = 3$ , we have reached the upper limit for the gains and should work within this range rather than trying to go beyond.



**Figure 8.** Output current w.r.t reference current for optimal gains.



**Figure 9.** Bode plot showing the response of  $I_2$  w.r.t  $I_{ref}$  for the optimal gains  $K_p = K_I = 1.65$ .

## 6. Conclusion and Future Work Include THD Output using FFT Analysis

We can use the proportional and proportional integral controllers to give the desired performance under utility THD below 5% for certain gains. But even in the range of gains that has been explored in this text, the controller performance is limited. PI controller is not a very good controller in the sense that it is not very effective at tracking a high frequency reference signal. The frequencies of our system and the controller to be used should be given special importance when choosing a particular controller and also its bandwidth.

We can control the d-q currents rather than the output current and compare their performances to establish which is more effective. The Repetitive Controller (RC) can be used to control the current either in simulation or by using a DSP based hardware platform. Also the study of RC by varying the grid frequency is also an interesting prospect for future work. The practical application of this model is in a Photo-Voltaic (PV) panels and in wind turbines which are connected to the grid through a suitable converter.

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