

Trend and Change Point Detection of Precipitation in Urbanizing Districts of Uttarakhand in India

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Abstract

Precipitation is the one of the prime indicators of climate change and its aberration causes many extreme events such as floods and droughts. Long-term trends were analyzed as monthly, seasonal and annual rainfall of Haridwar, Dehradun, Udham Singh Nagar, Almora and Nainital using Mann-Kendall and linear regression tests and change point was detected using cumulative deviation and Worsley likelihood statistic. Mann Kendall test revealed that there is significant increase in rainfall only for Haridwar district which has more urbanizing area compared to other districts. Haridwar is the holy place attracting significant floating population from all over the world, especially during festivals and fairs. Anthropogenic activity and industrialization is also the major cause of rainfall trend fluctuation in the Haridwar city. The monthly trend tests show that July rainfall is increasing whereas the December rainfall is decreasing which could be due to the seasonal shift. The start of change in the rainfall trend for the above mentioned districts is observed with distinct difference from 2009 onwards. From this it can be concluded that the stations to the west show significant trends compared to station which is towards east. Monsoon especially in July month a trend of increasing rainfall is observed in the studied Indian cities. The spatial and temporal trends of precipitation are pertinent for the future development and sustainable management of water resources of a given region.

Keywords: Change Point, Mann Kendall Trend, Rainfall, Uttarakhand, Worsely Likelihood Test

1. Introduction

Basic idea of rainfall pattern is required for a number of hydro meteorological applications like sustainable management of water resources, forecasting of drought and floods, planning for agriculture purpose, urbanization, modeling of hydrological feature, quantification of climate change impact, estimation of water balance and irrigation management for sustainable crop production¹¹. Rainfall is the one of the most important factors of hydro-meteorology that is severely affected by climate change impact². Prediction of rainfall characteristics is very difficult due to its variability both spatially and temporally²⁸. Variability of rainfall in hilly tract of Uttarakhand region is more due to its natural topography as well as anthropogenic effect²⁹. Yet there are number of researchers who tried to investigate the variability of rainfall, its pattern,

intensity etc. on a macro scale^{1,3,4} but the pattern of rainfall trend on small scale is still unexplored.

The changes in rainfall pattern have been reported by several researchers and predicted to change further². The Intergovernmental Panel on Climate Change (IPCC)⁵ reported the seasonal, annual and spatial variability in rainfall trends during the past few decades all across Asia. Numbers of studies have been carried out in various spatial and temporal scales. Many authors analyzed the rainfall patterns for several parts of India in a minor spatial scale^{8,24,26,33} and reported that there is no clear trend of increase or decrease in average rainfall over the country. Study conducted on all India scale (macro scale)^{10,15,24} indicated that intra-region variability for extreme monsoon seasonal rainfall is large and mostly exhibited a negative trend leading to increased frequency and magnitude of monsoon rainfall while the annual

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rainfall shows no significant trend except in the peninsular Indian region. Kumar and Jain¹⁸ carried out a detailed analysis to determine the trends in rainfall amount and the number of rainy days over major Indian River basins using daily gridded rainfall and reported that the six river basins had increasing trend in annual rainfall and 15 river basins had the decreasing trend, whereas the Ganga basin had no trend. Few studies have reported that the annual precipitation would increase in future in India for some particular months^{9,14,17,18,19,22}. Patra et al.²⁵ reported increasing trend during the months of January, August and September months in India.

There are number of parametric and non-parametric statistical test available to examine the trend of hydro meteorological parameters⁶. Parametric tests are more powerful as compared to non-parametric test but they require independent and normally distributed data series while non-parametric test requires only data to be independent data and they also have the ability to remove outliers. Most important and frequently test used for the analysis of rainfall trend is Mann Kendal (MK) Trend Test^{16,21} and Spearman's Rho (SR) which are frequently used in number of hydro meteorological studies^{17,31}. Comparative study of MK and SR shows that both the methods have similar capacity of detecting monotonic trends⁷.

The objective of this study is to determine the trend of rainfall on saptio-temporal basis in the selected district of Uttarakhand state which is most prone to high rainfall variability using Mann Kendall (MK) Test and Spearman's Rho (SR) Test trend test. Magnitude of slope was observed by using Thiel-Sen method^{30,34} method and change in trend is detected by using Worsely likelihood technique and CUSUM method. Change-point analysis was done to detect abrupt climate variations.

2. Study Area

Uttarakhand is situated in the foot hills of the great Himalaya lies between 28° 43' 31" 27' N and 77° 33' - 81° 02' E and famous for its recreational beauty of natural resources (Table 1; Figure 1). Uttarakhand has about 13 percent of its geographic area under cultivation, out of which about eighty percent of the land does not have assured irrigation facilities thus making agriculture crops totally dependent on vagaries of nature. The state situated centrally in the long sweep of the Himalaya,

forms a transitional zone between the per-humid eastern and the dry to sub-humid western Himalaya. The average annual rainfall of the state, as recorded is 1,547 mm. Altitude varies from 200 meter to more than 8400 meters from sea level. The temperature in hilly region goes occasionally below freezing point particularly during winter. The state comprises of two sub major division Garhwal and Kumaon with a total of 13 districts. More than 70 percent of population is directly or indirectly engaged in agriculture. This sector is poorly developed because of inaccessibility due to topographic condition and vulnerability of climate. As per the availability of long term data only five district of the state is selected in the study i.e., Haridwar, Dehradun, Almora, Nainital, and Udham Singh Nagar. Observed data of precipitation were acquired from Indian Metrological Department (IMD), Pune.

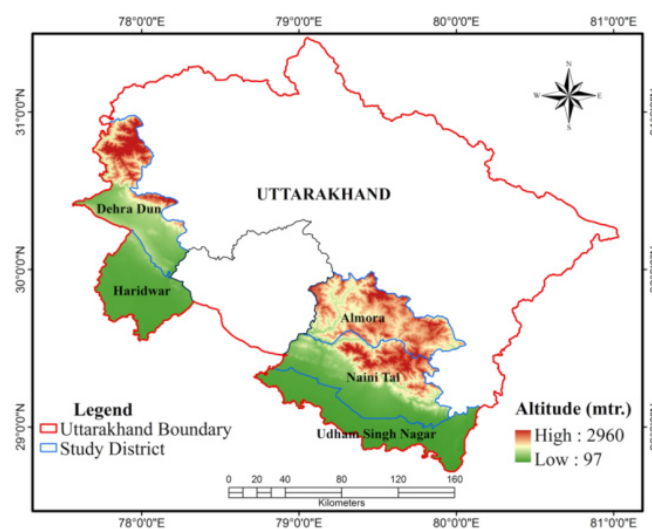


Figure 1. Demographic elevation map of study location in Uttarakhand.

Table 1. Details of study area of Uttarakhand in India

District	Lat	Long	Alt	Data Period	Rainfall (mm)
Almora	29° 37' N	79° 40' E	1651	1987-2011	1183
Haridwar	29° 58' N	78° 13' E	268	1979-2011	1015
Dehradun	30° 19' N	78° 04' E	640	1979-2010	2171
US Nagar	29°43'N	79° 70'E	550	1970-2010	1218
Nainital	29° 23' N	79° 30' E	2084	1980-2010	1493

3. Statistical Methods

3.1 Non-parametric Test

Non-parametric statistics are usually much less affected by the presence of outliers and other forms of non-normality²⁰. The most frequently used non-parametric test for identifying trends in hydrologic variables is the Mann-Kendall (MK) test. The statistical significance trend detected using a non-parametric model such as Mann-Kendall (MK) test can be complemented with Sen's slope estimation to determine the magnitude of the trend.

3.2 Mann-Kendall Trend Test

Mann Kendall statistics (S) is defined as²⁷ follows:

$$S = \sum_{i=1}^{N-1} \sum_{j=i+1}^N \text{sgn}(x_j - x_i) \quad (\text{i})$$

where, N is the number of data points. Assuming $(x_j - x_i) = \theta$, the value of $\text{sgn}(\theta)$ is computed as follows:

$$\text{sgn}(\theta) = \begin{cases} 1 & \text{if } \theta > 0 \\ 0 & \text{if } \theta = 0 \\ -1 & \text{if } \theta < 0 \end{cases} \quad (\text{ii})$$

It has been documented that when $n \geq 8$, the statistic S is normally distributed with the mean.

$$E(S) = 0 \quad (\text{iii})$$

The variance is written as-

$$\delta(S) = \frac{N(N-1)(2N+5) - \sum_{i=1}^m (t_i-1)(2t_i+5)}{18} \quad (\text{iv})$$

where, N is the number of ties group and t_i the number of data points in the t_{ih} tied group. Then Z -statistics computed¹² as:

$$Z = \begin{cases} \frac{S-1}{\sqrt{\text{Var}(S)}} & \text{if } S > 0 \\ 0 & \text{if } S = 0 \\ \frac{S+1}{\sqrt{\text{Var}(S)}} & \text{if } S < 0 \end{cases} \quad (\text{v})$$

Here Z follows standard normal distribution. A positive value of Z indicates upward trend and negative value indicate downward trend. A significance value α is utilized for testing either an upward or downward trend in a two sided test. If the Z value is greater than $Z_{\alpha/2}$, then null hypothesis (H_0) is rejected at a level of significance.

3.3 Theil-Sen's Estimator

The slope of n pairs of data points was estimated using the Theil-Sen's estimator^{30,34} which is given by the following relation:

$$\beta = \text{Median} \frac{x_j - x_i}{j - i} \text{ for all } i \leq j \quad (\text{vi})$$

In which $1 < j < i < n$ and β is the robust estimate of the trend magnitude. A positive value of β indicates an 'upward trend' while a negative value of β indicates a 'downward trend'⁰.

3.4 Spearman's Rho Test

Spearman's Rho is a rank-based test for correlation between two variables that can be used to test for correlation between time and the data series³². Spearman's correlation is a rank-based version of the usual parametric measure of correlation. In trend analysis; one variable is taken as the time itself (years) and the other as the corresponding time series data.

Like the Mann-Kendall Test, the n time series values are replaced by their ranks. The test statistic ρ_s is the correlation coefficient, which is obtained in the same way as the usual sample correlation coefficient, but using ranks:

Test statistics is defined by Siegel and Castellan³² as:

$$\rho_s = \frac{S_{XY}}{\sqrt{(S_X S_Y)}} \quad (\text{vii})$$

where,

$$S_X = \sum_{i=1}^n (X_i - \bar{X})^2$$

$$S_Y = \sum_{i=1}^n (Y_i - \bar{Y})^2$$

$$S_{XY} = \sum_{i=1}^n (X_i - \bar{X})(Y_i - \bar{Y})$$

And X_i (time), Y_i (variable of interest), x and y refer to the ranks (x , y , S_x and S_y have the same value in a trend analysis).

For large samples, the quantity $\rho_s = \sqrt{n-1}$ is approximately normally distributed with mean of 0 and variance of 1 (critical test statistic values for various significance levels can be obtained from normal probability tables).

3.5 Worsley Likelihood Ratio Test

The ratio test developed by Worsley³⁵ gives the jump in between the time series and this indicates the initiation of change. This method tests whether the means in two parts of a record are different (for an unknown time of change). The test assumes that the data are normally distributed.

$$Z_W = [K(n-K)]^{0.5} \times SS$$

$$Z_W = \frac{Z_w}{d_x}$$

Test statistics W is defined by Worsley³⁵ as:

$$W = \frac{(n-2)^{0.5} V}{(1-V^2)^{0.5}} \quad (\text{viii})$$

where,

$$V = \text{Max}|Z_w|$$

- n = No. of observations.
- K = weight assigned to SS
- SS = sum of squares
- W = Worsley Likelihood Ratio Test
- Z_w = Worsley Test statistic
- z_w = Test quotient
- V = any convenient statistic

The critical test statistic values for various significance levels for all selected observations are 2.869, 3.159 and 3.79 at 90, 95 and 99 % probability levels.

3.6 CUSUM Test

This method tests whether the means in two parts of a record are different (for an unknown time of change). It is a non-parametric test (distribution free). Given a time series data (X₁, X₂, X₃... X_n), the test statistic is defined as:

CUSUM change statistics (V_k) is defined by Inclan and Tiao¹³ follows:

$$V_k = \sum_{i=1}^k \text{sgn}(X_i - X_{\text{median}}) \quad (\text{ix})$$

where, k = 1, 2, 3,n.

$$\text{sgn}(X) = \begin{cases} 1 & \text{if } \theta > 0 \\ 0 & \text{if } \theta = 0 \\ -1 & \text{if } \theta < 0 \end{cases} \quad (\text{x})$$

X_{median} is the median of X dataset.

This is a rank-based test in which successive observations are compared with the median of the series⁷. The test statistic is the maximum CUMulative SUM (CUSUM) of the signs of the difference from the median (i.e. the CUSUM of a series of values of +1 or -1) starting from the beginning of the series.

4. Results and Discussion

4.1 Rainfall Characteristics

The rainfall characteristics of the study area are presented in Table 2 and Table 3. Mean annual rainfall is 1481.1 mm with a standard deviation of 197.7 mm. Monsoon rainfall contributes 78.8% and winter rainfall contributes 2.5% of the annual rainfall. During the monsoon season the coefficient of variation is very low (14.2%) compared to other seasons which shows a dependable monsoon rainfall. However, the spatial and temporal distribution of daily rainfall during monsoon season is very much uneven with either flooding or drought condition during the season. Figure 2 provides the Spatial Trend of Rainfall in the study area.

Table 2. Monthly rainfall trends and change points for Haridwar, Dehradun, Udham Singh Nagar, Almora and Nainital districts.

Rainfall Analysis - Haridwar 1979-2011									
Months	Trend statistics				Change statistics				Mean RF
	MK Test		Spearman's Rho		CUSUM		Worsley likelihood		
	Z	S	Z	Rho	Max Dev	YOC	W	YOC	
Jan	-1.26	-0.53	-1.3	-0.23	5	1983	2.33	2005	27.64
Feb	0.4	0.19	1.04	0.18	7	1987	2.19	1987	37.15
Mar	-0.31	0	-0.42	-0.08	3	2011	1.78	1982	24.57
Apr	-0.03	0	0.34	-0.06	6	2006	2.09	1983	17.17

May	1.32	0.71	1.27	0.23	6	1998	2.36	2010	36.01
Jun	-0.27	-0.2	-0.31	-0.06	5	1999	2	1999	103.3
Jul	2.16**	3.83	2.29**	0.41	7	2005	3.5**	2009	292.11
Aug	1.07	1.69	1.12	0.2	4	2008	2.07	1979	279.77
Sep	1.08	1.99	1.04	0.18	7	1987	2.19	1987	155.9
Oct	0.79	0	1.78	0.31	6	1994	1.3	1995	21.99
Nov	0.05	0	1.55	0.27	6	2002	2.65	1981	5.44
Dec	-1.4	-0.1	-1.19	-0.21	10*	1990	2.24	1990	14.11
Annual	1.90*	9.50	2.01**	0.55	6	1993	2.89*	2009	1015.2

Rainfall Analysis - Dehradun 1979-2010

Jan	-1.41	-0.95	-1.48	-0.27	5	2005	2.66	2005	42.98
Feb	0.05	0.026	-0.05	-0.01	3	1993	1.44	1979	57.4
Mar	-1.12	-0.625	-1.22	-0.22	3	2007	3.12*	1983	62.03
Apr	0	-0.002	-0.19	-0.03	4	1988	1.13	2002	32.61
May	0.21	0.218	0.25	0.04	5	1987	1.51	1996	66.51
Jun	0.08	0.29	-0.07	-0.02	5	2001	1.06	2008	227.96
Jul	1.67*	5.834	1.64*	0.29	6	1996	2.07	2009	633.16
Aug	0.44	1.322	0.5	0.09	3	1991	1.81	2009	685.8
Sep	1.83*	5.049	1.85*	0.33	6	1994	5.44***	2009	291.53
Oct	0.98	0.307	1.27	0.23	3	1995	1.24	1984	41.68
Nov	-0.82	0	-0.09	-0.02	3	2007	3.1	1981	8.54
Dec	-2.02**	-0.338	-1.74	-0.31	7.00*	1991	3.17**	1991	21.34
Annual	1.22	12.18	0.23	1.29	7.00*	1995	2.54	2009	2171.5

Rainfall Analysis - Udham Singh Nagar 1980-2010

	Z	S	Z	Rho	Max Dev	YOC	W	YOC	
Jan	-0.97	-0.213	-0.89	-0.61	4	2005	2.43	2005	28.02
Feb	0.6	0.133	0.67	0.12	4	1993	1.32	1983	36.32
Mar	-1.38	-0.333	-1.45	-0.27	4	1993	2.12	1982	21.91
Apr	-0.44	-0.1	-0.43	-0.08	4	2001	1.67	1986	20.41
May	1	0.653	1.03	0.19	6	1997	1.94	1997	42.85
Jun	1	2.28	0.96	0.18	6	1999	3.01*	1999	179.13
Jul	-0.22	-0.747	-0.31	-0.06	5	2006	2.25	1988	422.95
Aug	1.58	5.358	1.82*	0.33	8**	2001	2.42	2002	422.67
Sep	1.22	3.75	1.37	0.25	3	1996	2.44	2009	263.05
Oct	-0.04	0	0.63	0.12	5	2006	1.11	1999	35.69
Nov	0.27	0	1.75*	0.32	5	1988	0.97	1988	4.41
Dec	-3.01	-0.706	-2.47**	-0.45	10*	1991	2.88*	1991	15.96
Annual	1.19	11.42	0.23	1.29	3	2006	2.43	2002	1493.4

Rainfall Analysis - Almora 1987 - 2011

Jan	-1.65	-1.427	1.65*	-0.34	5	2005	2.97*	2005	41.2
Feb	-0.63	-0.705	0.7	-0.14	2	1990	1.09	1990	63
Mar	-1.24	-1.231	-1.32	-0.27	3	2007	2.19	1993	44.8
Apr	-0.35	-0.29	-0.32	-0.07	2	2008	1.96	1988	38.3

Table 2. (Continued)

Rainfall Analysis - Haridwar 1979-2011									
Months	Trend statistics				Change statistics				Mean RF
	MK Test		Spearman's Rho		CUSUM		Worsley likelihood		
	Z	S	Z	Rho	Max Dev	YOC	W	YOC	
May	0.58	0.657	0.68	0.14	3	2007	2.18	2005	73.4
Jun	0.77	1.801	0.77	0.16	2	2010	1.92	2010	156.6
Jul	1.14	2.933	1.15	0.23	4	2006	2.53	2009	267.8
Aug	0	-0.02	0	0	3	2009	3.06*	2010	286.2
Sep	1.1	2.638	1.12	0.23	3	1997	1.86	2009	165.1
Oct	1.59	0.576	1.82	0.37	5	2003	2.12	1995	21.8
Nov	0.31	0	0.81	0.17	5	2005	1.04	1999	6.9
Dec	-1.15	-0.239	-1.21	-0.25	5	1991	3.54**	1991	18.2
Annual	1.28	6.421	1.15	0.23	4	2006	2.53	2009	1183.2
Rainfall Analysis - Nainital 1970 - 2010									
Jan	-0.83	-0.266	-0.69	-0.11	4	2005	2.28	2005	40.9
Feb	0.98	0.553	1.1	0.17	8**	1989	1.89	1999	55.9
Mar	-0.18	-0.09	-0.22	-0.03	4	1983	1.59	2007	46.3
Apr	1.83**	0.667*	1.90**	0.30	4	1993	2.94*	1981	37.8
May	0.69	0.423	0.72	0.11	5	1996	2.17	1971	61.6
Jun	0.04	0.046	0.1	0.02	4	1995	1.86	2008	136.2
Jul	-0.33	-0.35	-0.16	-0.03	6	1979	1.68	2009	265.2
Aug	0.89	1.273	0.82	0.13	5	2006	1.93	2006	269.9
Sep	1.57	3.403	1.56	0.25	10*	1997	2.56	2004	219.9
Oct	-1.05	-0.27	-0.71	-0.11	6	1975	1.71	1985	56.4
Nov	1.12	0	2.40**	0.38	5	1988	1.35	1978	9.5
Dec	-0.23	0	0.29	0.05	6	1991	1.39	1997	18
Annual	1.36	6.179	1.41	0.22	6	2001	1.35	2006	1217.5

Table 3. Critical values of MKTT, Spearman's Rho, CUSUM and Worsley likelihood tests at different levels of significance.

Level of Significance	Tests of Trend and Change Point Detection			
	MKTT (Z)	Spearman's rho (Z)	CUSUM (Max Dev)	WorselyLikelihood (W)
*** = 0.01	2.576	2.576	7.114	3.790
** = 0.05	1.960	1.960	7.930	3.160
* = 0.10	1.645	1.645	9.504	2.870

4.2 Haridwar

MK Trend of monthly rainfall and year of change between the periods 1979 to 2012 was examined by using the equation (i-v) and equation (vi) respectively for Haridwar district revealed that negative trend was observed for January, March, April, June and December month with

both the tests but the value was statistically not significant. While February, May, July, August, September, October and November was having positive trend examined with both parametric tests. But the trend was only significant for July month. Sen's slope indicated that the rate of change in July rainfall was 3.83 mm/year. Significant

change point for this trend was detected as year 2009 by Worsley likelihood technique (equation –viii) while year 2005 was detected by CUSUM technique (equation- ix and x) but the value was not significant. CUSUM has detected a significant change point for December but the corresponding trend result of this month was insignificant. Annual rainfall for this station has significant increasing trend as stated by both methods and the year of change was observed as 2009.

4.3 Dehradun

Trend statistics of the Dehradun station from the period 1979–2010 was detected and revealed that negative trend was observed for January, March, November and December month but the change was significant for December month only. Positive trend of rainfall was observed for the month of February, April, May, June, July, August, September and October but the value was statistically significant for July and September month. The rate of change for this two month was 1.67 and 1.83 mm/year. Significant change point for December month rainfall was detected as year 1991 by CUSUM and Worsley likelihood method. Although four significant changes point (March, July, September and December) in a year has been carried out by Worsley likelihood method but corresponding trend was significant for September and December only. Sen’s slope estimate shows that the significant rate of change for December month was very minimal i.e. 0.3

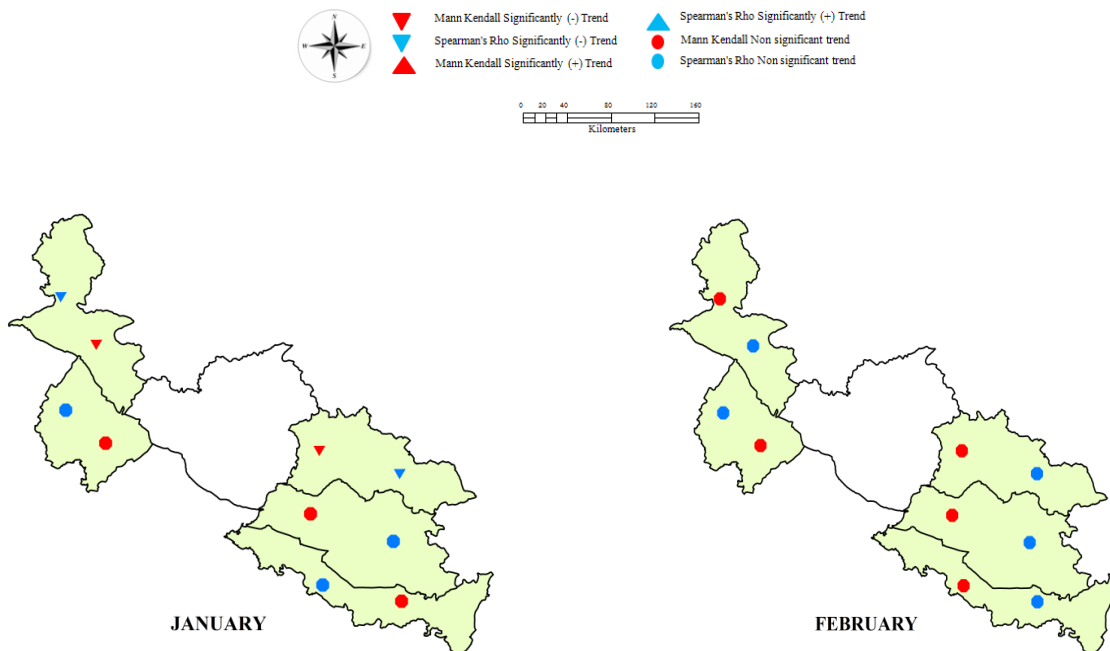
mm/year while for September and December it was 5.8 and 5.0 mm respectively. Annual rainfall for this station have positive trend but the statistics is not significant. Abrupt change in annual rainfall was detected from 1995 by CUSUM method.

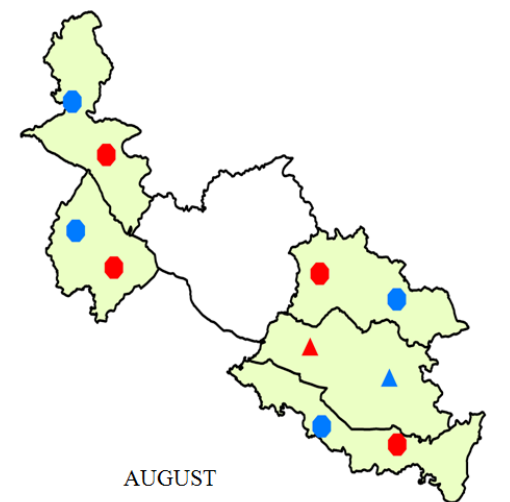
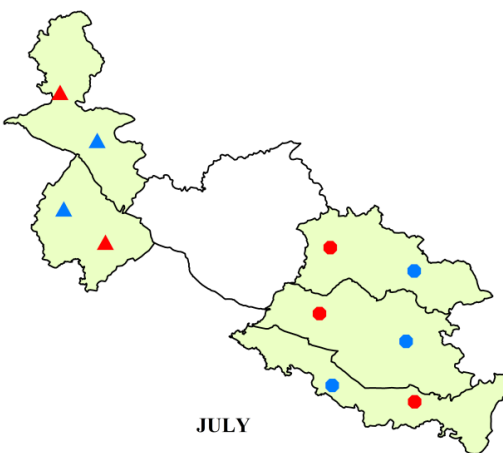
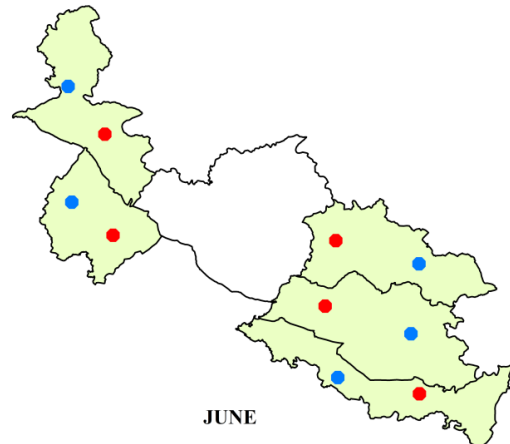
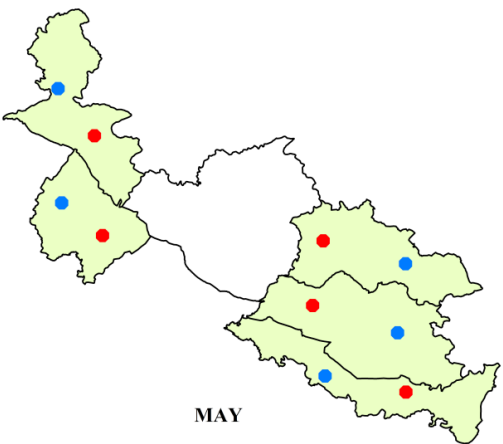
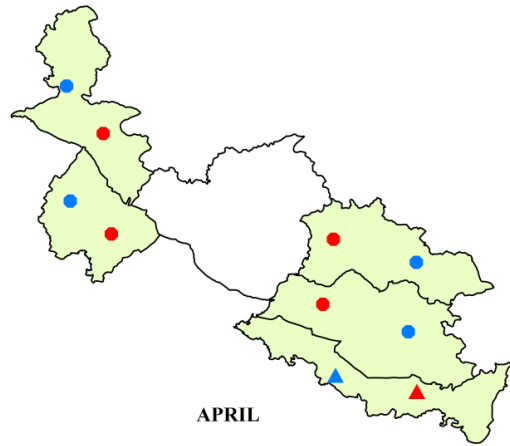
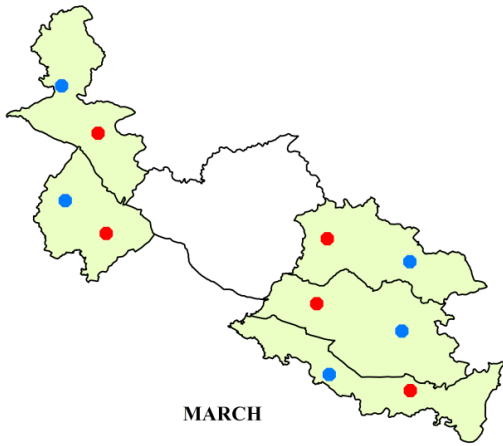
4.4 Udham Singh Nagar

Rainfall data analysis from the period 1980-2010 revealed that total six month i.e. January, March, April, July, October and December) have negative trend of rainfall; whereas positive trend was observed for February, June, August, September and November month. The trend was statistically significant for December month by both the methods and change point for that particular month was detected as 1991. Significant positive trend for the month August was detected by Spearman’s Rho method but the trend was not significant with MK Test; whereas change point for this month was year 2001. Not significant trend was observed for annual rainfall.

4.5 Almora

Rainfall data analysis pertaining to Almora station from the period 1987–2011 revealed that trend statistics for January, February, March, April and December having negative trend by both methods while May, June, July, September, October and November having positive trend.





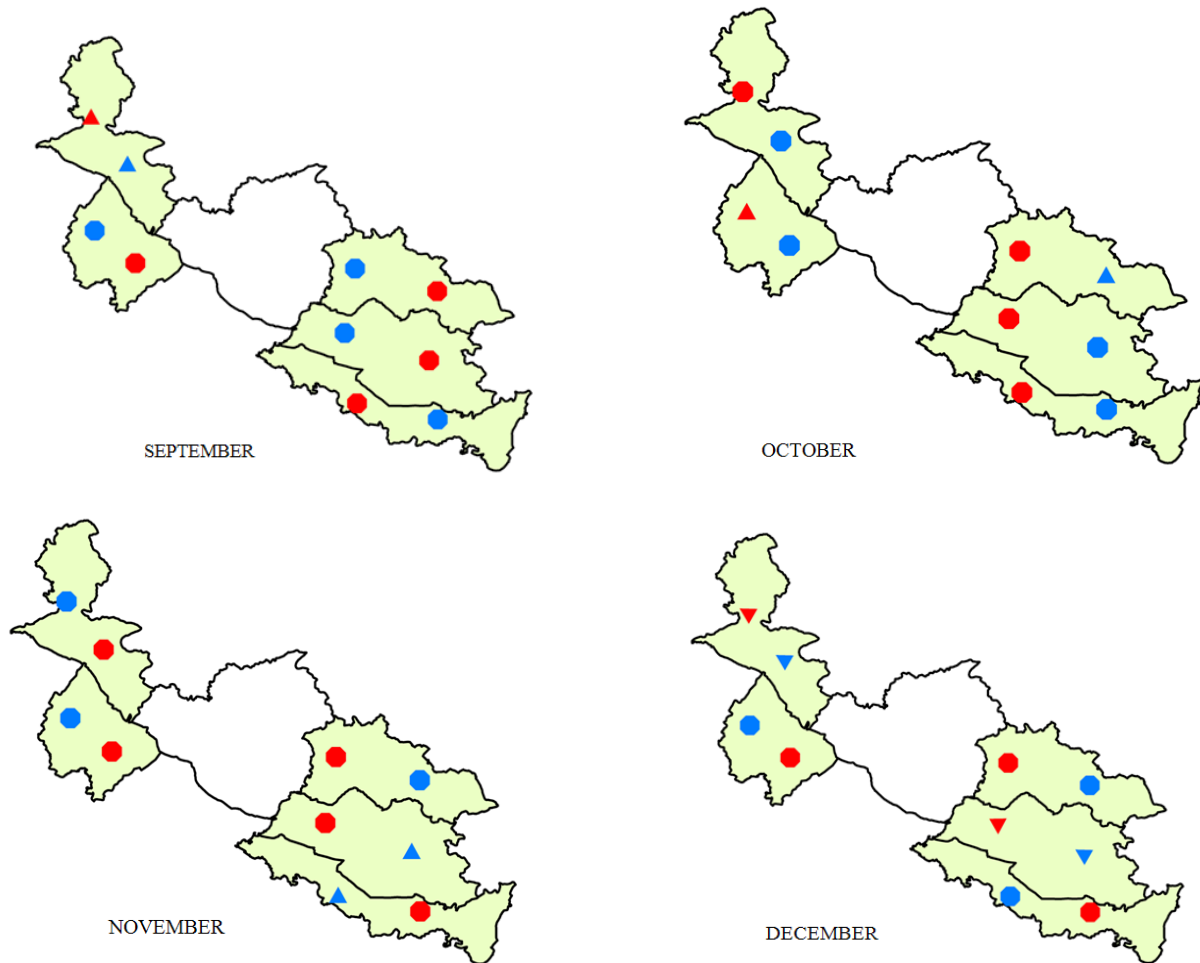


Figure 2. Spatial Trend of Rainfall in the study area.

5. Conclusion

Long term rainfall over study area, was analyzed for temporal trend at monthly and annual basis. The investigation showed a long term insignificant declining trend of annual as well as monsoon rainfall, whereas an increasing trend in post-monsoon season. During monsoon season the monthly rainfall in the June, July and September months were found to be in decreasing trend, but there was increasing trend in the month of August. The trend is even more evident in last 10 years. Though the analyzed trends might be statistically insignificant in nature, it has high practically significant effects in managing resources and agricultural activities over the region. In this study mainly focused on long variation of trend with different level of significance and change point detection of the time series. Whereas, the shorter period of recent data set showing higher significance may have better practical utility assuming

a better explanation of accelerated change in climate pattern and thus have greater impact on natural resources. Trend and change point detection techniques is very fruitful for future prospective i.e., irrigation as well as water resources planning and associated with real world problem.

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